Going green: Agent-based modeling of the diffusion of dynamic electricity tariffs

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Going green: Agent-based modeling of the diffusion of dynamic electricity tariffs

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Abstract
Using an agent-based modeling approach we show how personal attributes, like conformity or indifference, impact the opinions of individual electricity consumers regarding switching to innovative dynamic tariff programs. We also examine the influence of advertising, discomfort of usage and the expectations of financial savings on opinion dynamics. Our main finding is that currently the adoption of dynamic electricity tariffs is virtually impossible due to the high level of indifference in today’s societies. However, if in the future the indifference level is reduced, e.g., through educational programs that would make the customers more engaged in the topic, factors like tariff pricing schemes and intensity of advertising will became the focal point.

Keywords: Dynamic pricing, Time-of-use tariff, Demand response, Diffusion of innovations, Agent-based model.

JEL: C63, O33, Q48, Q55

1. Introduction

In the not so distant past, the construction of the power system was hierarchical. Electrical energy was generated mostly from fossil fuels, like coal or lignite, in large conventional power plants. Then, the electricity was delivered via transmission and distribution lines to end users. The position of the consumers – companies and households – was passive. Their awareness and knowledge of energy consumption levels was generally limited to the bills paid at the end of the month.

Nowadays, the power systems are decentralized to a large extent. Competition has been allowed on the level of generation and sales of energy in the wholesale and retail markets. This
has created new challenges to be faced by market participants and regulators. The biggest one is probably the threat that demand and supply of electricity will not match in the coming future. On one hand, energy demand is increasing rapidly and – according to experts – further growth will be observed due to increased ‘electrification’ of our lives and population growth (BP, 2012; Birol, 2004; ExxonMobil, 2013). Energy demand has become also more sophisticated: the consumers are more aware of their rights and they want a reliable supply of electricity of good quality. On the other hand, due to the constantly decreasing natural resources the generation may face problems of scarcity in supply of fossil fuels. On top of that most of the present generation and transmission infrastructure (i.e., power plants, transmission lines, etc.) is old and inefficient. Among other challenges is the increasing presence of renewable energy sources (RES) in the power system, like wind, solar and hydro energy. The non-dispatchable, non-controllable character of most of these sources influences both the supply and demand in the power system (Harris, 2006; Kirschen and Strbac, 2004; Shively and Ferrare, 2010).

The way in which the power system will develop is defined to some extent by policy makers. One of the most crucial legal regulations that has a great impact on the future of the power system, is the Climate Policy 3 × 20 (EC, 2007). It obliges governments of the EU countries to design appropriate energy policies, which will lead to a reduction in CO₂ emissions and an increase in the participation of renewable energy in the market. Moreover, energy efficiency must be increased. There are also EU Directives that have a great, strategic impact on the development of the power system. For instance, Directive 2012/27/EC that establishes a common framework of measures for the promotion of energy efficiency within the EU in order to ensure the achievement of the EU’s 2020 20% headline target on energy efficiency and to pave the way for further energy efficiency improvements beyond that date (EC, 2012). In particular, this directive requires the introduction of meters that would provide feedback to private households on energy consumption and information about energy efficiency. Moreover, energy suppliers are obliged to offer electricity tariffs that would motivate households to conserve energy or shift electricity consumption from peak to off-peak periods (EC, 2012; Paetz et al., 2012).

The important question that arises in this context is whether the households will switch to the new – more energy-efficient but less comfortable – dynamic tariffs and how fast or slow will this process take place. Using an agent-based modeling approach, in this paper we show how personal attributes, like conformity or indifference, impact the decisions of individual electricity consumers. We also examine the influence of mass-media education programs and the expectations of financial savings on the decision making process.

The paper is structured as follows. In Section 2 we discuss the position of the electricity consumer and describe the new possibilities, connected with the current legal regulations and the development of innovative information and communication technologies (ICT). We also comment on the results of some pilot programs that have been run recently in Europe and the U.S. The aim of these programs was to evaluate the attitude of the electricity consumer to particular demand response tools. In Section 3 we introduce our agent-based model and present the Monte Carlo simulation scheme. We also discuss the position of our model in the rich universe of agent-based models of social influence. In Section 4 we present the results of our extensive simulation study. Finally, in Section 5 we conclude, discuss policy implications and comment on future work.
2. Consumers in today’s electricity markets

In the last couple of years, the position of electricity consumers in the power system has radically changed. Due to market decentralization and the presence of a growing number of renewable energy sources (RES) on the lower voltage levels, new possibilities have arisen for the consumers. They can now play an active role in the power system. They have the right to change the energy supplier (as a result of the Third Party Access policy, see Diaz-Rainey and Tzavara, 2012; EC, 2009) and to choose a specific pricing program. Moreover, they can now relatively easily start to generate energy and use it for their own needs or sell the surplus to the distribution system operators. In this way they can become prosumers, i.e., consumers, who consume and produce energy at the same time.

The ambitious goals set by the EU will have a great impact not only on power generation but also on consumption. As the power system of the future has to be more sustainable, built on a greater energy efficiency and a high share of renewable energy, the changes will certainly impact the households. In order to increase energy efficiency, the consumers will need to decrease their electricity consumption and may need to make new investment in more efficient home appliances. Furthermore, they will be required to shift loads, which may also involve changes in everyday behavior and routines (FORSA, 2010; Jongejan et al., 2010; Paetz et al., 2012). Increased efficiency of energy usage should result in cost savings (electricity demand shifted to the time zones when the electricity price is lower, decreased total amount of energy consumption, energy saving home appliances, etc.). On the other hand, new investment cost may be necessary, for instance, cost of smart meters, smart appliances, smart plugs, etc.

Due to the mentioned structural changes, the economic relationships between market participants are becoming more sophisticated and require a fresher look. As a result, a new approach has been proposed recently. The so-called Smart Grids use modern communication technologies to exchange information between market agents (generators, market operators and end-users) in order to improve the efficiency of energy production and consumption (see e.g. Jackson, 2010; Palensky and Dietrich, 2011; Zhang and Nuttall, 2011). The information gathered by smart meters can be used to improve the market structure and increase the competitiveness of the energy sector (Darby, 2006, 2010). The popularity of the Smart Grids concept induces discussion on the role of consumers in the power system. By the means of advanced but already available information and communication technologies (ICT), consumers can have tools that will enable them to control their electricity consumption on a daily basis.

One of the crucial challenges of the coming years is to optimize the use of existing capacity while meeting ever-increasing demand for electricity and reducing CO₂ emissions. It seems that this could be achieved at a relatively low cost by introducing Demand Side Management (DSM) and Demand Response (DR) instruments (Darby and McKenna, 2012; Faruqui, 2012; Gerpott and Mahmudova, 2010; Strbac, 2008; Zugno et al., 2013). The DSM/DR tools are designed to influence consumption patterns and energy efficiency of end-users and therefore to reduce energy production and load variability. The literature considers DSM/DR instruments ranging from education (encouraging efficient usage of energy), through time-based pricing (time-of-use rates, critical peak pricing, real-time pricing) to incentive-based DR (direct load control, emergency demand response programs, capacity market programs). Among the DSM/DR tools, dynamic tariffs
are one of the most common and interesting.

2.1. Dynamic pricing programs

So far most of residential electricity consumers have conventional electricity meters that measure only the total electricity consumption. The majority of consumers use simple one- or two-time zone tariffs (flat tariffs, like days and night tariffs) and are even not aware what kind of a tariff they have and what impact on their energy costs it has. A typical energy demand curve shows two peaks: one in the morning and another one, more pronounced in the Winter (or cold season), in the afternoon-evening hours, see Figure 1. Dynamic tariffs have been invented to flatten the curve and to shift the demand from on-peak hours to off-peak hours. On one hand, the shift of load implies a change in consumers’ habits and daily routines; sometimes it may be connected with the reduction of the overall energy consumption. On the other, it reduces the imbalance between peak demand and peak supply and helps to manage the power supply costs. Furthermore, it is expected that the flattened energy demand curve will lower the general operation costs of the distribution system operators and lead to a reduction of wholesale power market prices (Procter, 2013).

Dynamic tariffs differ a lot from typical or traditional tariffs. In a variable electricity tariff, the price of electricity is dependent on the balance between supply and demand in the market. With such a tariff the consumer may experience several changes in price levels during the day due to the fluctuations of supply and demand (Faruqui, 2012; Gerpott and Paukert, 2013; Strbac, 2008; Thorsens et al., 2012; Zugno et al., 2013). Among variable electricity tariffs, the following can be distinguished (Darby and McKenna, 2012; Ehlen et al., 2007; Faruqui and Sergici, 2010; Jongejan et al., 2010):

- **Time-of-use pricing** (TOU) – within this tariff the electricity prices are divided into a couple of time zones, depending on the time of usage: the electricity price during on-peak hours is higher than the price during off-peak hours. The goal is to flatten the load curve by reducing on-peak demand and increasing off-peak demand.
• **Critical peak pricing** (CPP) – in this tariff on-peak times are limited to just a few days per year, when demand is expected to be the highest, such as during a heat wave in the Summer or a cold spell in the Winter. CPP on-peak electricity prices typically range between 400% and 700% of the off-peak electricity price. The idea behind CPP tariffs is to create a financial incentive to reduce electricity consumption during extremely high demand days.

• **Peak-time rebate** (PTR) – this tariff offers a rebate to customers who reduce their electricity demand on critical peak days.

• **Real-time pricing** (RTP) – within this tariff the electricity price is dependent on the actual real-time costs of electricity based on supply and demand (e.g., the power exchange spot price). By means of advanced ICT solutions, consumers are informed in real-time about the electricity price. This tariff is rarely chosen by electricity consumers, as it is too uncomfortable to monitor the constantly moving price of electricity. The only reasonable solution is to use automatic smart appliances.

Innovative advanced technologies like ARM (*automated meter reading*) and AMI (*advanced metering infrastructure*) are necessary to enable implementation of dynamic pricing programs and extended usage of other DSM/DR tools. In most cases, a so-called enabling technology is needed to increase the positive impact of a dynamic tariff on the energy demand. Such an enabling technology is an equipment that enables the customer to automate control of the load consumption according to the specific price and time ranges. Moreover, it ensures transparency of electricity prices. Such enabling technologies include smart meters, in-home displays, smart thermostats, web based consumer portals, smart plugs/appliances or home area networks (Faruqui and George, 2005; FORSA, 2010; Gerpott and Paukert, 2013; Jongejan et al., 2010; Paetz et al., 2012; Star et al., 2010). A dynamic tariff is not a modern product, but when combined with enabling technologies, advanced ICT technologies, it can become a real innovative solution, which may eventually conquer the market.

2.2. **Pilot programs in the U.S. and the EU**

In the recent years, a number of pilot programs, focused on the reduction of peak demand and energy conservation at the consumption level, have been run in the U.S. and in Europe (Ehrhardt-Martinez et al., 2010; Faruqui, 2012; Jongejan et al., 2010; Peters et al., 2009; Sopha et al., 2011; Star et al., 2010). Many experiments were conducted in an attempt to understand consumers’ responsiveness to variations in retail electricity prices (Allcott, 2011; ATKearney, 2012; Faruqui and George, 2005; Faruqui and Sergici, 2010; Grans et al., 2013; Ozaki, 2011; Thorsens et al., 2012).

It has been shown that in the case of flat tariffs the electricity demand is price inelastic. On the other hand, implementation of time-of-use rates (TOU) or critical-peak pricing (CPP) programs increases price elasticity over time, due to consumers’ gradual adaptation of daily routines to the new tariffs. TOU rates induce a drop in peak demand that ranges from 3% to 6%, while CPP tariffs induce a drop in peak demand from 13% to 20%. However, the elasticity level depends on climate conditions, seasons of the year, income levels and appliance ownership (Faruqui and Sergici, 2010; Thorsens et al., 2012).
When accompanied by enabling technologies, the introduction of TOU rates leads to a drop in peak demand up to 15% and of CPP rates to a drop in peak demand up to 44% (Ehrhardt-Martinez et al., 2010; Star et al., 2010). Moreover, according to ATKearney (2012) and Darby and McKenna (2012), a reduction of energy consumption increases from 5% to 10% with enabling technologies. Enabling technologies greatly improve the overall impact of demand response and significantly increase the savings in both avoided capacity and avoided electricity for the utility. The main problem with this solution is that the cost of the enabling technologies is currently higher than potential savings (Gerpott and Paukert, 2013; Jongejan et al., 2010; Paetz et al., 2012).

In many experiments, the conventional electricity meters were replaced with smart meters. Together with in-home displays they were used as a source of information for customers about the real energy consumption. The information was also provided to the clients in an indirect way, via billing. It has been shown that energy conservation and reduction of peak demand increases because of receiving better information about electricity consumption (in a direct or/and an indirect way), see Darby (2006); Ehrhardt-Martinez et al. (2010); Gerpott and Paukert (2013); Grans et al. (2013); Matsukawa (2005); Thorsens et al. (2012).

Although promising results have been achieved in many pilot programs, another problem has been defined. Namely, only a small amount of participants of the pilot programs decided to sign up for the new tariffs. For instance, in Illinois in the AIU Power Smart Pricing Program only 18% of customers, where the pilot program was run, were aware of it. Moreover, only 10% of them understood the program and only 5% were interested in the program. In the end, under 1% of customers enrolled in the program (Star et al., 2010). Lack of interest and fear of change were named as the main reasons for such low program participation rates (ATKearney, 2012; Darby and McKenna, 2012).

What is interesting, is that such results were obtained in countries like the U.S., Canada, U.K. and Germany, where the population was generally aware of and sensitive to issues related to energy efficiency, smart grids and dynamic pricing. In those societies pilot programs have been run for years, and most people should have been familiar with those terms and issues. However, according to a survey conducted in 2010 in the U.K. only 8% of respondents think that energy needs ‘attention and improvement’ (OFGEM, 2010). The report of ATKearney (2012) provides even more dramatic numbers: 60-75% of consumers are not aware of the existence of smart grids and are not willing to shift their consumption to off-peak hours. Similar results have been obtained in Germany (FORSA, 2010; Gerpott and Paukert, 2013; Paetz et al., 2012). For example, in project MeRegioMobil, which is part of the broad EU project Internet of Energy, currently run in six German regions (BMWi, 2012), the customers’ attitude towards dynamic pricing programs and smart technologies has been evaluated. The results of the analysis have shown that as long as the consumers are not familiar with the new technologies and are not aware of the potential energy and cost savings, they will not be interested in changing anything in their daily routines. Their basic lack of knowledge is responsible for their indifference to the energy market and energy efficiency. Most people are not interested in changing the energy supplier and looking for another attractive pricing program (Paetz et al., 2012).

The level of awareness, understanding and interest is even lower in Central and Eastern European (CEE) countries. For instance, knowledge and awareness is estimated at 24% in Poland compared to 49% in the U.S. Smart grids, energy efficiency or demand response tools are rather
new in CEE and very few people are familiar with these terms. However, first pilot programs have been started. In most of these programs, conventional electricity meters have been replaced with smart meters. Consumers are also trained how to use smart meters for a more rational and conscious use of energy (AT Kearney, 2012).

Promoting a sustainable use of electricity can be difficult, because electricity differs from other consumer goods. As mentioned by Fisher (2007) and Hargreaves et al. (2010), it is invisible and untouchable and consumed indirectly by related activities. However, when people are informed their interest increases and most of them gain a positive attitude towards DR tools and smart technologies. Their main motivation for a potential change of the energy seller or the pricing program is cost savings. Environmental benefits are seen as positive side-effects. On the other hand, people have doubts about the real potential of these savings. They would prefer to get all the necessary equipment (e.g., smart meters, home-displays) for free. In case, when they need to invest their own money, they want to get a fast payback from these investments. The biggest disadvantage for them is the possible reduction in comfort by rescheduling the daily routine in response to electricity prices dictated by the variable electricity tariff (FORSA, 2010; Paetz et al., 2012). To reduce this disadvantage a typical energy consumer would like to have enabling technologies, that adjust work of the home appliances according to the price level of electricity. Moreover, to increase the participation and engagement rates, the non-economic or one-off incentives, like an offer of a free programmable thermostat, could be helpful (Darby and McKenna, 2012; Faruqui and Sergici, 2010; Peters et al., 2009). To reach a high level of enrollment, the design of the pricing rate, education and marketing of new solutions and offerings must be appropriate. Without that, there will be no significant demand response as a result of the lack of knowledge, high level of indifference and ignorance of the consumers.

3. Model description

3.1. Historical background

In the last two decades, agent-based computational economics (ACE) has become a widely accepted approach to solving both theoretical and practical problems in economics in general (Cincotti et al., 2008; Farmer et al., 2012; Hommes, 2006; Squazzoni, 2010; Tesfation, 2003) and energy economics in particular (Bunn and Martoccia, 2005; Bunn and Oliveira, 2001; Cincotti and Gallo, 2013; Ehlen et al., 2007; Guerci et al., 2010; Jackson, 2010; Sun and Tesfatsion, 2007; Zhang and Nuttall, 2011). The basic tool of ACE – an agent-based model (ABM; sometimes referred to as a ‘multi-agent system/simulation’) – is a class of computational structures and rules for simulating the actions and interactions of autonomous agents (both individual or collective entities, such as organizations or groups) with the ultimate objective to assess their effects on the system as a whole.

For a couple of decades, scientists have been proposing models for describing how a new product, like the iPhone or the iPad, enters the market. This class of problems is called diffusion of innovations and has been extensively studied to date, starting with the classical works of Rogers (1962) and Bass (1969), continuing through the second half of the XX century and in recent-day publications, see Goldenberg et al. (2007, 2010); Kiesling et al. (2011); Nyczka and Sznajd-Weron (2013); Przybyła et al. (2013); Weyant (2011) to name a few. Interestingly, nearly all models
describing the diffusion of innovations have a common feature: the adaptation behavior of the agent is represented by means of a single dichotomous variable taking the values $-1$ (potential adopter, customer of the old product) or $+1$ (adopter, customer of the innovative product).

Such agents have been used in statistical physics for almost a century and are referred to as spins (Ising, 1925). Initially spins have been introduced to understand the magnetic properties of a physical system. However, spins turned out to be a useful concept for many interdisciplinary applications; already three decades ago Galam et al. (1982) used it to model social collective behavior. In sociophysics – a statistical physics approach to social systems (for a recent, comprehensive review see Galam, 2012) – the term spin is used interchangeably with the term agent. Both typically represent dichotomous variables (‘binary individuals’).

On the other hand, the field of agent-based modeling has developed considerably since the pioneering work of Schelling (1971) and nowadays in economics agents are often described by more complex structures than simple binary variables. In general, agents can be characterized by many traits, can have their own strategies, etc. To distinguish these more ‘complex’ agents from their ‘simpler’ cousins a new term – spinson – has been used recently by Nyczka and Sznajd-Weron (2013) and Przybyła et al. (2013) to describe a particularly simple agent that is characterized by a single binary ($\pm 1$) trait. The term spinson is derived from two words: spin and person. Graphically it is a combination of an arrow (a spin) and a person (head and body) as in Figs. 2-3. In this paper, we will interchangeably use the terms spinson, agent, customer, individual and household to represent a simple agent that is characterized by a single binary ($\pm 1$) trait. By using the terms referring to the more complex variables and structures, we want to emphasize the fact that our model is just a ‘simple spinson model’ of the complex reality with interacting agents, customers, individuals or households.

In this paper, we focus on the process of adoption of electricity consumers to a new dynamic tariff. As in the classical diffusion of innovations theory (Bass, 1969; Rogers, 2003), as well as in ACE studies (Moldovan and Goldenberg, 2004; Goldenberg et al., 2007, 2010), in our model the new product adoption is driven by two forces:

- **Internal influence** that comes from the interactions between consumers (e.g., word of mouth). In our case the nature of these interactions is motivated by the psychological observation of the social impact and has been introduced originally in (Sznajd-Weron and Sznajd, 2000) to describe opinion dynamics.

- **External influence** (or external field), which in our case describes not only the marketing efforts (advertising, promotions, etc.) but also product features (potential savings, comfort/discomfort of usage of a particular tariff, etc.).

Before going into details, let us stress two main differences between our model and other models of diffusion of innovations (Bass, 1969; Moldovan and Goldenberg, 2004; Goldenberg et al., 2007, 2010):

- In classical models and many recent ABM models, the transitions between the states are assumed to be irreversible. The customers cannot ‘un-adopt’ after adoption to the new product, i.e., once they switch to the new electricity tariff they cannot return to the original
one even if the new tariff turns out to be unsuitable for them. In our model the reversal to the original product is possible.

- In most diffusion of innovations models, the internal and external influences are given by some constant parameters, i.e., there is some probability $p$ that in a certain time period the individual will be influenced by the external factor and probability $q$ that the he/she will be affected by the neighbor(s). In our model the form of internal interactions comes from social motivations (discussed in the following section).

3.2. Model construction

We consider a set of $i = 1, .., N$ spinsons on a square grid (i.e., a chessboard). Each spinson represents a household and is characterized by its attitude $S_i$ toward an innovative dynamic electricity tariff. If $S_i = -1$ the household prefers a traditional uniform tariff, if $S_i = +1$ it prefers the new dynamic tariff. At a given time $t$, the opinion of a particular spinson depends on three factors:

- **Conformity**, which represents a specific response to interactions (e.g., word of mouth) between the spinson and its neighbors. The neighborhood can be interpreted in terms of either physical or social connection. As in Sznajd-Weron and Sznajd (2000) the nature of these interactions is motivated by the psychological observations of the social impact dating back to Asch (1955): if a group of spinson’s neighbors unanimously shares an opinion, the spinson will also accept it, see Fig. 2.

- **Product features**, which are modeled by a global field, as in Sznajd-Weron and Weron (2003, 2008), see Fig. 3. The strength of the field depends on features of the new dynamic electricity tariff: potential savings, (dis)comfort of usage, intensity of advertising, etc.

- **Indifference**, which introduces indetermination in the system through an autonomous behavior of the individuals (Boudon and Bourricaud, 2003). In the case of indifference the spinson is immune to the influence of the neighbors and the field, see Fig. 4.

The concept of indifference requires a further explanation. In the general sense, the word indifference denotes the lack of importance, care or concern, but can be also related to the autonomy of the individuals. In the agent-based model of Przybyla et al. (2013) such an autonomy was due to the so-called independence, which is one of the possible responses to social influence and denotes a particular type of non-conformity. The level of independence can be connected with the level of individualism in the society (Hofstede, 2001) and in most cases is expected to be rather low. An autonomous behavior can be also reflected by indifference, as noted by Boudon and Bourricaud (2003). They argue that it can arise if two products (e.g., traditional and dynamic electricity tariffs) offer both advantages and disadvantages and these advantages and disadvantages are not clearly comparable. In such a case, the strategy finally adopted by an individual is broadly unpredictable. There is also a third interpretation of indifference, related to its general meaning. In this case, it expresses insignificance and is not directly related to a particular product (e.g., tariffs) but reflects the importance or popularity of the whole topic in the society (e.g., energy saving, ecology).
Figure 2: Interactions between spinsons (representing households in our model) are described by the social influence of the unanimous majority. With probability \((1 - p)\) a randomly chosen agent (the one in the circle) follows the state (or shares the opinion) of the \(2 \times 2\) panel (the one in the middle) if it is unanimous. If the panel is not unanimous the spinson is responsive to the external force, see Fig. 3.

Figure 3: External force (or external field) represents product features like potential savings, (dis)comfort of usage, intensity of advertising, etc. It has an effect on spinsons only if they are not indifferent. With probability \((1 - p)\) a randomly chosen spinson (the one in the circle) is responsive to the field if the \(2 \times 2\) panel is not unanimous. With probability \(h\) the spinson adopts to the advertised product (right) and with probability \((1 - h)\) it remains unchanged (left).

Figure 4: Indifference is introduced to the model as a kind of noise and represents (temporary) resistance to word of mouth and global advertising. With probability \(p\) a randomly chosen spinson \(i\) (the one in the circle) flips \(S_i(t + dt) = -S_i(t)\) with probability \(f\) (right) or remains unchanged \(S_i(t + dt) = S_i(t)\) with probability \(1 - f\) (left), independently of the state of the \(2 \times 2\) panel and the external force.
We wish to emphasize that the broad concept of *indifference* plays a central role in our model. We introduce it mainly to reflect the dependence of the diffusion of the new product on its perception and social significance. In energy markets, consumers are often confused and unable to evaluate electricity tariffs. There are a few causes for this confusion:

- The tariff consists of a few components (electricity, transmission, services, etc.). The price of each component is calculated differently and for most of users it is not clear how the final sum is computed.
- Agents do not have the information about their consumption patterns nor the knowledge about the power consumption of equipment. Therefore, they cannot easily calculate potential savings.
- The new tariffs are associated with a hard to quantify discomfort in usage of home appliances. It is hard to compare financial gains with discomfort resulting from shifting the consumption to off-peak hours.

Moreover, consumers do not consider tariff selection as an important and interesting issue. OFGEM (2011) analysis indicated that the majority of panel participants could be classified as ‘disengaged’, meaning that they neither knew their tariffs nor were willing to change them. Star et al. (2010) obtained similar results on the basis of a market survey: one of the reasons of low enrollment in the pilot program in Illinois was disinterest (respondents did not want to complicate their lives, were happy how things were). To sum up, electricity consumers cannot evaluate different tariff features and generally are not interested in the problem. Hence, they are characterized by a high indifference level.

On the contrary, when products like smartphones or tablets are considered, a low indifference level is observed. The conforming behavior results from two facts: different models are easy to compare and high-tech products are perceived as symbols of social status. People willingly discuss and compare new phones, laptops, etc., and hence are more susceptible to the opinions of others.

### 3.3. Spinson dynamics

The behavior of a randomly chosen spinson $i$ at time $t$ is illustrated in Fig. 5. First, we check whether the spinson is indifferent to social pressure. With probability $p$, i.e., if $r_1 < p$ for a randomly generated uniform number $r_1 \sim U(0, 1)$, the spinson is indifferent and not interested in discussing electricity tariffs; with probability $(1 - p)$, i.e., if $r_1 > p$, the spinson is likely to be influenced by the opinions of his neighbors. Similarly as in the model proposed by Przybyla et al. (2013), we assume that the behavior of the indifferent spinson is characterized by the flexibility parameter $f$, describing how frequently the spinson changes its opinion, see Fig. 4. In the simulations, for simplicity we set $f = 0.5$, but it has been shown that for any value of $f > 0$ the simulation results can be rescaled using the remaining model parameters (Przybyla et al., 2013). It should be noted that the behavior of an indifferent spinson is in some sense not rational (the spinson may not even bother to check the features of the two tariffs) and purely random. Hence, the existence of indifference introduces noise into the system. Moreover, under indifference, the system never reaches an absorbing steady state, in which all agents share the same opinion.
If the spinson is not indifferent, its opinion may be subject to change due to the social pressure of its neighbors. In this case, in the second step a neighboring 2×2 panel of four spinsons is chosen randomly. If the opinion of the panel is unanimous, spinson \( i \) follows the opinion of the panel, see Fig. 2. On the other hand, if the panel is not unanimous, then the spinson will be exposed to the influence of the external field (i.e., product features). For simplicity, we assume that the external field is uniform and can affect all spinsons in the same way. The strength of the field is described by the parameter \( h \). It defines the probability with which the spinson can be convinced to switch to the new dynamic tariff because of its features. Consequently, with probability \( (1-h) \) the spinson will stay unconvinced, see Fig. 3. The strength of the field depends on the particular tariff: expected bills and potential savings, (dis)comfort of usage, intensity of advertising, etc.

3.4. Simulation setup

In the simulation, we run \( M \) experiments. A single experiment consists of \( T \) Monte Carlo steps (MCS), which can be interpreted in terms of time intervals (e.g., days). In each MC step, \( N \) elementary sub-steps (illustrated in Fig. 5) are repeated. The number of the sub-steps is equal to
the size of the population \( (N) \) to ensure that on average each spinson is chosen once in a single MCS. As the outcome of a single MC simulation experiment \( m \) we compute the ratio \( c_m(T) \) of spinsons in favor of the new dynamic tariff after time \( T \) to the total number of spinsons \( N \) in the system

\[
c_m(T) = \frac{\#\{i : S_i(T) = 1\}}{N}
\]

where \( m = 1, \ldots, M \). Next, we compute the average of the ratios of convinced spinsons over \( M \) experiments

\[
c(T) = \frac{1}{M} \sum_{m=1}^{M} c_m(T)
\]

The results depend on the length of simulation \( (T) \) and the parameter values \((p, f \text{ and } h)\). The longer the time horizon, measured by \( T \), the closer is the system to the stationary solution. The influence of the simulation parameters \((p \text{ and } h); \text{note that flexibility } f = 0.5 \text{ is fixed in our study}) \) will be discussed in the following section.

In the simulations, we use the following specifications:

- Initially all spinsons are down, i.e., \( c(0) = 0 \). This corresponds to a situation in which the innovation is still not available, so no one can be a consumer of the new product.

- The population inhabits a square lattice \( 100 \times 100 \) and consists of \( N = 10000 \) spinsons. It is worth to mention that other system sizes were also investigated and all results presented in this paper are consistent with those for other lattice sizes.

- We count the number of convinced spinsons after \( T = 720 \) Monte Carlo steps, which corresponds to a two year period. Longer and shorter time horizons were also investigated, for a detailed discussion see Przybyła et al. (2013).

- The results are averaged over \( M = 1000 \) experiments.

4. Results

4.1. Pre-simulation expectations

Before moving on to discuss the simulation results, let us ask ourselves what can we expect of the model. Usually some predictions or expectations can be deduced from a heuristic analysis of the model. Performing this step prior to running the experiment can be considered as a ‘best practice’ of social studies (Myers, 2006). Recall, that in our model three factors influence a spinson’s opinion:

- social validation (conformity) that should be responsible for increasing homogeneity in the society and is present in any social system,

- external field \( h \) that forces spinsons to choose the new product (i.e., a dynamic electricity tariff),
Figure 6: Simulation snapshots showing a sample time evolution of a system of 100 × 100 spinsons for the initial concentration of spinsons $c(0) = 0$, indifference $p = 0.01$ and the external field $h = 0.11$. As a result of social influence (e.g., word-of-mouth) small clusters of convinced (dark green) appear. Some of these clusters disappear (hollow arrows) and other – if a critical size is reached – spread like a virus (filled arrow).

- indifference that introduces indetermination, which is always present due to a non-zero level of independence, and might increase in case of uncertainty or irrelevance.

Based on this knowledge, at least two conjectures can be formulated:

1. The number of convinced individuals should gradually increase with the level of the external field $h$.
2. In our model, an innovation cannot spread in the society if there are no autonomous spinsons. Imagine that initially all spinsons are down, i.e., all consumers use the old product (traditional electricity tariff). If the level of indifference is zero ($p = 0$), the changes in the system can be caused only by social validation or the external field. However, if all spinsons have the same opinion conformity always works due to the very strong social pressure and there is no influence of the external field (see Fig 5). Therefore, indifference is needed to break unanimity.

The dependence between the number of convinced individuals and the level of indifference is not easy to predict. It may have ambiguous effects. On one hand, the indifference boosts the diffusion process, by weakening the social pressure. On the other hand, it introduces noise, which reduces the impact of the external field. Hence, the indifference may hamper the spread of new ideas.

4.2. Model performance

Let us first consider the general performance of the model, for both low and high values of indifference. In Figure 6 we present snapshots showing a sample time evolution of the system of
100 × 100 spinsons, initially all preferring the traditional tariff \( c(0) = 0 \), having a low level of indifference \( (p = 0.01) \) and influenced by a relatively weak external field \( (h = 0.11) \). As a result of social influence (e.g., word-of-mouth), small clusters of convinced (dark green) appear. Some of these clusters disappear and other (if a critical size is reached) spread like a virus. Notice that after time \( T = 210 \) a small cluster of 73 spinsons appeared (indicated by a hollow arrow). After further 90 steps (i.e., for \( T = 300 \)) it disappeared. Then at time \( T = 455 \) two clusters formed – one of 78 spinsons (indicated by a hollow arrow) and another of 147 spinsons (indicated by a filled arrow). The former one disappeared (90 steps later it is not visible anymore), while the latter one started to spread like a virus.

This is an interesting phenomenon that cannot be obtained within classical theories of the diffusion of innovation (like the Bass, 1969, model) and may correspond to the important feature of real-world systems known as the valley-of-death (Weyant, 2011). On the other hand, a cluster of 147 spinsons that formed after \( T = 455 \) MCS was able to grow and spread in the society. It seems that if some critical size of the cluster is crossed, the innovation is able to spread in the society, which agrees with the critical mass theory (Rogers, 2003) – a crucial concept in understanding the social nature of the diffusion process.

Note also that in classical models and many recent ABM models (see Kiesling et al., 2011, for a review) the transitions between the states are assumed to be irreversible. The customers cannot ‘un-adopt’, even if the new product (here: the dynamic tariff) turns out to be unsuitable for them. In our model, the reversal to the original product is possible. The vanishing clusters in Fig. 6 show that a group of convinced spinsons can loose its interest in the new dynamic tariff and after a short period of time can be again in favor of the traditional flat tariff.

For \( p > 0 \) the dependence between the number of convinced individuals and the indifference level \( p \) is highly nontrivial (see the left panel in Fig. 7). It can be noticed that for very small values of \( p \), which are associated with problems of a great social importance and interest, a given strength of the field is not sufficient to encourage consumers to accept a new offer. It seems that in such a case, consumers behave conservatively and prefer to use previously known products. Strong incentives are needed to change their attitude. As the level of indifference increases, the ratio of convinced spinsons jumps to almost 1.

This indicates that a minimum level of autonomy is necessary to ensure that the new idea spreads in the population. To some extent this result is in agreement both with the concept of innovators and the critical mass theory. Innovators play a central role in the innovation diffusion theory, which says that some individuals decide to adopt an innovation independently of the decisions of other individuals in the social system (Bass, 1969). The critical mass theory says that some threshold of individuals or actions has to be crossed before a social movement explodes into being (Rogers, 2003; Granovetter, 1978; Oliver and Marwell, 1985).

Moreover, for a small value of indifference there is a critical value of the external field, above which an innovation can spread in the market (see the right panel in Fig. 7), which also is in agreement with the critical mass theory. Recalling our first conjecture about the dependence between the number of convinced spinsons and the external field, we are in a position to grasp the complexity of the system described by a relatively simple ABM model. We have expected a gradual growth of convinced spinsons with the increase of the external field \( h \) ... and this is not true, at least for small levels of indifference. This means that for issues of high social relevance or interest
Figure 7: *Left panel:* Dependence between the ratio of convinced spinsons (customers) after two years (which corresponds to 720 MCS) and the level of indifference $p$ for several values of the external field $h$. *Right panel:* Dependence between the ratio of convinced after two years and the external field $h$ for several values of indifference $p$. As discussed in Section 2, today’s retail electricity markets are characterized by high levels of indifference, i.e., $p > 0.5$. However, if in the future the indifference level is reduced, the external field (i.e., tariff pricing schemes, advertisements, etc.) will become the focal point.

A certain threshold has to be crossed in order to adopt a new idea. Moreover, once the threshold is passed, further increase of the external field does not result in a significantly higher number of convinced, which can be seen in the right panel of Fig. 7 for indifference levels $p = 0.01$ and $0.1$. For high indifference levels ($p > 0.5$), the ratio $c$ of convinced spinsons is much less sensitive to the model parameters – indifference $p$ (see the left panel in Fig. 7) and external field $h$ (see the right panel in Fig. 7). In the limiting case of $p = 1$, the opinions are purely random because neither the internal factors (like word-of-mouth) nor the external field influence individuals. Therefore in such a case, independently of the level of the external field, the ratio of convinced spinsons $c$ converges to 0.5. This result might seem paradoxical at first; it suggests that 50% of consumers prefer dynamical tariffs. However, one should remember that for $p = 1$ the opinions are very unstable. At a certain moment of time, a given spinson can have an opinion $\downarrow$, in the next changes it to $\uparrow$, then back to $\downarrow$ and back again – it flips up and down randomly. Hence, a spinson’s opinion fluctuates a lot. This reflects more the general indifference to the topic than the attitude toward a new idea.

This high variability is illustrated in Figure 8, where we present snapshots showing the configurations of systems after $T = 720$ MCS, evolving from the initial concentration $c(0) = 0$ for the same intensity of the external field ($h = 0.11$) but two different values of indifference. For low indifference ($p = 0.01$; left panel), there is a cluster of convinced, which will eventually spread throughout the whole system. Moreover, if we would follow the time evolution of the system it would behave similarly to the one presented in Fig. 6. The convinced spinsons very rarely flip to the unconvinced state (light gray) or back again and therefore only small fluctuations can be observed in the system. A completely different behavior is observed for high indifference ($p = 1$; right panel). Of course, initially the whole system is gray (all spinsons are $\downarrow$) because $c(0) = 0$. Yet nearly instantly the spinsons start switching back and forth, due to their autonomous behavior.
As a result the system looks qualitatively the same for the rest of the time evolution.

Let us now summarize the general Monte Carlo simulation results. First of all, our expectations put forward in Section 4.1 are fulfilled only partially. Indeed, an autonomous behavior (i.e., $p > 0$) is needed for the diffusion of innovation, which agrees with classical theories (Rogers, 2003). However, the dependencies between the ratio $c$ of convinced and parameters $p$ (indifference) and $h$ (external field) are highly complex. We have expected that the ratio of convinced would gradually grow with the increase in the intensity of the external field. However, this is true only for intermediate levels of indifference. For low values of $p$, there is a critical value of the external field below which there is no diffusion of innovation and above which all consumers are convinced independently of $h$. For example, if $p = 0.1$ then for $h < 0.09$ there is no diffusion and for $h > 0.09$ the ratio $c$ is almost 1, see Fig. 7 and the two left panels in Fig. 9. On the other hand, for large values of $p$ the number of convinced grows gradually with $h$, but the growth is surprisingly weak, see Fig. 7 and the two right panels in Fig. 9. Moreover, it was not easy to predict ex-ante the dependence between the ratio of convinced and indifference, and indeed this dependence is not obvious. As already mentioned, for $p = 0$ the ratio of convinced $c = 0$. Then it increases and reaches a maximum, which is $h$-dependent, to finally drop to 0.5, independently of
4.3. Diffusion of electricity tariffs

Let us now focus on the diffusion of dynamic electricity tariffs. As discussed before, the retail electricity market is characterized by:

- high values of indifference, i.e., \( p > 0.5 \), which expresses the fact that electricity tariffs are not a very popular discussion topic in the society and are hard to compare (i.e., are a source of confusion),

- a weak external field, i.e., \( h \) close to 0, which reflects the rather small potential savings, the significant discomfort of adopting a new dynamic tariff and the generally low level of advertising and lack of educational campaigns related to these products.

On the other hand, the results discussed in Section 4.2 show that the external field, which describes important features of the tariff, plays a significant role only for relatively small values of indifference. As long as the indifference level is high, the ratio of convinced depends very weakly on the strength of the field. In the right panel of Figure 7, the curve representing the ratio \( c \) of convinced spinsons is very flat for \( p = 0.8 \) and becomes only slightly steeper for lower indifference levels, like \( p = 0.6 \). This indicates that even large changes in the strength of the field will have very small effects on the diffusion process. For instance, the difference between the ratios of convinced spinsons for \( h = 0.05 \) and \( h = 0.4 \) is 3.7% for \( p = 0.8 \) and 1.7% for \( p = 0.9 \). Hence, we may conclude that in the context of electricity tariffs, which are nowadays characterized by high values of \( p \), the features of the tariffs have a limited impact on their popularity.

The results of Section 4.2 also indicate that the ratio of convinced can increase even if the external field is fixed. The left panel in Figure 7 shows that the reduction of indifference level from a very high (more than 0.5) to moderate (around 0.2) could result in a significant growth of the ratio of convinced customers. If we analyze a market with a weak external field, say \( h = 0.05 \), then the ratios for \( p = 0.8, 0.5 \) and 0.2 are \( c = 0.506, 0.531 \) and 0.790, respectively. The change is not only quantitative but also qualitative. For the same field intensity and a smaller indifference level, the opinions will become more stable and will not fluctuate so often. It is an important feature, if we want to consider not only the diffusion of opinions but also analyze the resulting decision process, which is known to be a very complex phenomenon (Myers, 2006). It is very likely that customers need some sense of certainty before they take an action, like signing up for a new dynamic electricity tariff.

Finally, note that the independence between the product quality and the ratio of convinced cannot be achieved under a classical modeling approach. If all agents behave rationally and maximize their utilities, they should respond to the product features. Hence, one could expect that attractive products would gain popularity. In the proposed setup, the introduction of indifference enables modeling of consumer irrationality. This feature of our model is especially important in the context of the retail electricity market because it has been observed (see the discussion in Section 2) that new tariffs remain unpopular regardless of their attractiveness.
5. Conclusions, policy implications and further research

In this paper, we have presented the results of an extensive simulation study on the diffusion of dynamic tariffs in the retail electricity market. We would like to emphasize that the agent-based model (ABM) we have used is based on established knowledge from social sciences. As in other diffusion of innovations studies (Kiesling et al., 2011; Rogers, 2003), in our model the new product adoption is driven by the internal influence that comes from interactions between agents (e.g., word of mouth) and the external field, which describes not only marketing efforts (advertising, promotions, educational campaigns, etc.) but also product features (potential savings, comfort/discomfort of usage of dynamic electricity tariffs, etc.). The assumptions of our model, related to the social influence of neighbors, colleagues or friends, are based on numerous social experiments and observations (Asch, 1955; Bocchiaro and Zamperini, 2012; Myers, 2006). What distinguishes our model among others, is the way, in which we define the immunity of some agents to the social influence. As noted by Boudon and Bourricaud (2003), the so-called indifference – connected with an autonomy of individuals – can arise if two options (e.g., traditional and dynamic electricity tariffs) offer both advantages and disadvantages and these advantages and disadvantages are not clearly comparable. In such a case the strategy finally adopted by an individual is broadly unpredictable. Because such an uncertainty is very strong in the case of electricity tariffs (AT Kearney, 2012; Darby and McKenna, 2012; OFGEM, 2011; Star et al., 2010), we have introduced indifference as a kind of randomness into the model. Moreover, social experiments show that people are inconsistent in their behavior and simple situational factors are more powerful than individual traits in shaping human behavior (see Bocchiaro and Zamperini, 2012, for a review). This fact is reflected in our model by the probability of indifference – in each time step an agent can be indifferent or susceptible with some probability and its behavior changes in time.

For a model to be trusted, it has to reproduce empirical facts. One of the best-established stylized facts in the field of diffusion of innovation is the $S$-shaped curve representing the time change of the number of consumers having adopted to a new product. As already shown by Przybyła et al. (2013), the model used in this paper reproduces this fact perfectly. In this paper we have additionally shown that the model is able to describe two other phenomena that are crucial for the diffusion of innovation – existence of the so-called critical mass (Granovetter, 1978; Oliver and Marwell, 1985; Rogers, 2003) and the valley-of-death (Weyant, 2011). These results are particularly important, because neither the critical mass nor the valley-of-death effect can be obtained within classical theories of the diffusion of innovation (like the Bass, 1969, model). Moreover, they show that, in spite of its simplicity, our model reproduces properly the most important features of the diffusion phenomenon.

The most important conclusion from this study is the following: The adoption of dynamic electricity tariffs is virtually impossible due to the high level of indifference in today’s societies. For a high level of indifference, the fluctuation of an agent’s opinion leads to his/her inability to make a decision and switch to a new dynamic tariff, no matter how strong is the influence of the external field. And high levels of indifference and disengagement of the consumers, who neither have knowledge about electricity tariffs nor are willing to change them, have been confirmed by many independent studies (AT Kearney, 2012; OFGEM, 2011).

Therefore, in light of the results of our model and of the pilot programs conducted in Europe
and the U.S., we can derive an important policy recommendation: *If the indifference level of the retail consumers is not reduced, the efforts to smooth the electricity demand via dynamic tariffs will not bring the expected results.* In order to overcome this problem, utility companies should cooperate with the policymakers, governments and ecological organizations. A public debate is needed. When customers engage more in the topic, the adoption of dynamic electricity tariffs will be much more likely. Finally, if in the future the indifference level is reduced, the external field (i.e., tariff pricing schemes, advertisements, etc.) will become the focal point, see Fig. 7.

The research can be extended in various ways. Firstly, the presented approach can be used to explain and model the free rider problem (Diaz-Rainey and Tzavara, 2012). If we allow for a heterogeneous field, we will be able to distinguish regular customers from free riders. Free riders are people, who anticipate the externalities, such as a change of future electricity prices or the state of the environment due to other agent actions. Hence, they take into account possible profits, which arise when other customers change their attitude into more economical or ecological, while evaluating the advantages and disadvantages of a new tariff. Therefore, the product features, such as possible savings or effects on the environment, will have a much weaker effect on their opinions. We predict that the presence of the free riders in the model can slow down or even stop the diffusion process.

Finally, we can expand our agent-based model, in order to explain and analyze the differences between the opinions and decisions. It is well known that there are big discrepancies between customers’ opinions stated in market surveys and their actual participation in pilot programs and acceptance of new tariffs (Darby and McKenna, 2012; Star et al., 2010). Our analysis already sheds some light on the problem. We have shown that due to the high indifference level in today’s retail electricity markets, the agent opinions are very unstable and change frequently. This may hamper the decision process, because consumers typically need some sense of certainty before they take any actions. It seems that reducing the indifference level can result in narrowing the gap. Potentially it can even lead to the reverse situation, where the number of customers, who switch to the new tariff, will be larger than the number of people, who currently are in favor of dynamic tariffs.

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