

# Introduction to Mathematical Modelling

## Question List 1.

*Golden ratio. Fibonacci numbers. Principle of mathematical induction*

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1. What is the golden ratio?
2. Give three geometric constructions of the golden ratio.
3. What are the golden rectangle and the golden spiral? Draw the picture.
4. What are the golden triangle, the golden gnomon, and the golden pyramid?
5. Draw a pentagram and indicate three pairs of segments in it which constitute the golden ratio.
6. Define the following sets of numbers: natural, integer, rational, real.
7. Is the golden ratio a rational number? Explain the answer.
8. What is the definition of the Fibonacci numbers? What is their relation to the golden ratio?
9. Give the formula for the  $n$ -th Fibonacci number.
10. Give the formula for the sum of squares of first  $n$  Fibonacci number. What is the Fibonacci spiral? Draw the picture.
11. Formulate the Principle of Mathematical Induction.
12. What is the definition of a general linear regression?
13. What is the characteristic polynomial for a linear regression? What is the characteristic polynomial for Fibonacci numbers? Specify its roots.
14. What is the algorithm to deduce a formula for the  $n$ -th element in a linear regression?