Mathematical Analysis II Question List for the Midterm.

- 1. Domain and graph of a function of several variables
- 2. Partial of a function of several variables: definition, examples.
- 3. Directional derivatives: definition, relation to the partial derivatives.
- 4. Gradient, its relation to partial and directional derivatives.
- **5.** The formula of small increments
- **6.** The tangent plane to a graph of a function: definition, equation.
- 7. Higher order partial derivatives: definition, examples.
- 8. The Schwartz lemma.
- **9.** The Hessian of a function: definition, relation to second derivative of a section of a function in a given direction.
- 10. Sufficient condition for local convexity/ concavity.
- 11. Positive/negative definiteness of a symmetric matrix: definition and the Sylvester criterium.
- 12. Local extrema: definition and necessary condition in the terms of the gradient
- 13. Classification of critical points. Sufficient conditions for a critical point to be a local minimum/local maximum
- 14. Local extrema under given constraints: definition, the Larange multipliers method